Maths Circle India: Module 8, Session 2 Organized by Indian Statistical Institute Session Date: 3rd February, 2023

1 Division

- (a) Let a and b be two positive integers. Show that there are integers q and r such that b = qa + r, where r = 0 or 0 < r < a.
- (b) Now let a be a positive integer and b be any integer. Show that there are integers q and r such that b = qa + r, where r = 0 or 0 < r < a.
- (c) Now let a and b be two integers wherea is negative. Show that there are integers q and r such that b = qa + r, where r = 0 or 0 < r < -a.